FXHIBIT"A"

RANSPORT PHENOMENA

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the definition of the friction factor we have obtained the result that finary by using arguments similar to those in §6.2. Hence from the dimensional analysis of the partial differential equations describing the flow and from BEST AVAILABLE COPY

be carrelated as a function of Re alone.

increase in the amount of eddying behind the sphere. The kink in the curve separation zone from in front of the equator to in back of the equator of $Re = 2.1 \times 10^3$. In this system, as the flow rate increases, there is an at about Re = 2 x 10° is associated with the shift of the boundary-layer this system there is no sharp transition from an unstable (aminar flow curve. Many experimental data have been taken for flow around spheres, so that a charl of f versus Re is available for smooth spheres. (See Fig. 6.3-1.) For to a stable turbulant flow curve as was indicated for tubes in Fig. 6.2-2 at

We have purposely chosen to discuss the sphere immediately after the tube in order to emphasize the fact that various flow systems may behave quite differently. Several points of difference between the two systems are: For spheres the f-curve exhibits the sphere.

For tubes there is a rather well-defined leminar-turbulent transition at

For smooth tubes the only contribution to f is friction drag. Rc = 2 × 103.

For spheres there are contributions

transition,

to fowing to both friction drag

no well-defined laminar-turbulent

For tubes there is no boundary layer separation.

remembered.

.e .e feurve associated with a shift Kink For spheres there is a

and form drag.

the separation zone.

Por the creeping flow region, we already know that the drag force is given by Stakes's law, which is a consequence of an analytical solution of the equations of motion and continuity (with the term $\rho D v/D t$ amitted from the The general shape of the curves in Figs. 6.2-2 and 6.3-1 should be carefully By rearranging Stokes's law (6.3-19)Tq. 2.6-14) in the form of Eq. 6.1-5, we get equation of motion given in Eq. 3.2-20). Fr = TR - 1 puo

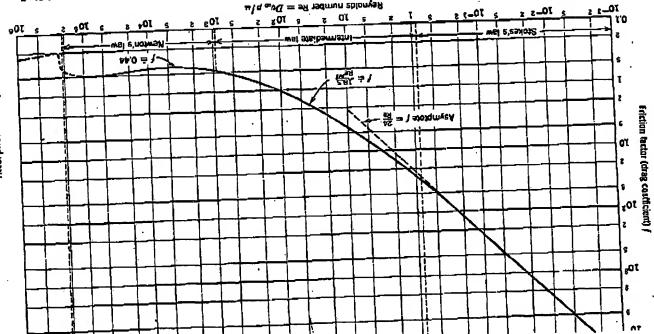
Hence, for creeping flow around a sphere.

Rc < 0.1 212

This is the straight-line portion of the $\log f$ versus $\log \mathrm{Re}$ curve.

• See H. Schlichting. Boundary Layer Theory. McGraw-Hill, New York (1955), pp. 34-3:

Hill, New York (1950), Third Edicion, p. .8-1.8 Curve saken from C. "Dust and Mist Collection," in Chemical Engineers' Hondback by 1. H. Perry).



Interphase Transport in Bothermal Systems

higher values of the Reynolds number, it is very disticult to make theoretical calculations. Several investigators have managed to the seurve for Re > 0.1 is a result of experiment. Occasionally, te f as far as Re = 10 but only with a considerable amount of effort. analytical expressions for the higher Reynolds number regions are For the intermediate region, we may wille very approximately

$$= \frac{18.5}{R_{\rm ph} T_{\rm i}} \quad 2 < R_{\rm 0} < 5 \times 10^{3} \tag{6.3-21}$$

indicates a lesser dependence on Re than in Stokes's law. This

higher Re, we see that the friction factor is approximately constant.

to the square of the velocity of the fluid moving past the sphere. region the drag force acting on the sphere is approximately proporhat Newton's "faw" for the drag force on a sphere is not to be confused on 6.3-22 is a useful approximation for making rapid estimates.

fects (see Problem 6.0), fall of droplets with internal circulation,3 particles in non-Newtonian fluids,4 bindeced settling (i.e., fall of y extensions of Fig. 6.3-1 have been made, but a systematic study be beyond the scope of the text. Among the effects investigated are of particles which interfere with one another), wasteady flow,

spheres of density Aph = 2.62 g cm⁻⁸ are allowed to fail through carbon wide (p = 1.59 g cm 2 and p = 9.38 millipoises) at 20° C in an experiment fing reaction times in making time observations with stopwatches and more e devices. What diameter should the spheres be to order to have a terminal Imb, Hydrodynamics, Dover (1945), Sinh Edition pp. 600-601; S. Hu and R. C.

Steinout, Ind. Etg. Chem., 34, 618-624, 840-847, 900-901 (1947); see also C. E. Finid and Parlicle Dynamics, University of Delaware Press, Newark (1951), of about 65 cm sec-1?

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Imb, Bydradynamics, Dover (1943), Siath Edition pp. 600-601; S. Hu as A.C.L.E. Journal, 1, 42-48 (1955).

Slattery, doctoral thesis, University of Waconsin (1959).

Stelatout, Ind. Eig. Chem., 36, 618-624, 840-847, 900-901 (1947); see al. Child and Parilicle Dynamics, University of Delawara Press, Newarth 13.

Palyjohn and E. R. Gilfiland, Chem. Erg. Prog., 49, 497-504 (1952).

See Becker, Can. J. Chem. Erg. 77, 85-91 (1959).

Friction Factors for Flow around Spheres

However, in this equation one has to know D in order to get f; and f is given by the solid curve in Fig. 6.1-1. A trial-and-error procedure can be used, taking To find the sphere diameter, we have to solve Eq. 6.1-7 for D. f = 0.44 as a first guess.

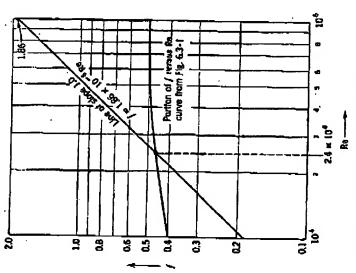


Fig. 6.3-2. Graphical procedure used in Example 6.3-1.

Alternatively, we can solve Eq. 6.1–7 for f and then note that f/Re is a quantity independent of D:

$$\frac{f}{Re} = \frac{4}{3} \frac{g\mu}{\rho \nu_o^3} \left(\frac{\rho_{\rm gh} - \rho}{\rho} \right) \tag{6.3-23}$$

The quantliy on the right side can be calculated with the foregoing data, and we can call it C. Hence we have two simultaneous equations to solve;

$$f = CRe$$
 (from Eq. 6.3-23) (6.3-24)
 $f = f(Re)$ (given in Fig. 6.3-1) (6.3-25)

(6.3-25)Equation 6.3-24 is a straight line of alope unity on the log-log plot of f versus Re. (given in Flg. 6.3-1)

For the problem at head,

$$C = \frac{4(980)(9.58 \times 10^{-9})}{3(1.59)(65)^3} \left(\frac{7.62 - 1.59}{1.59}\right) = 1.86 \times 10^{-6} \tag{6.3-26}$$